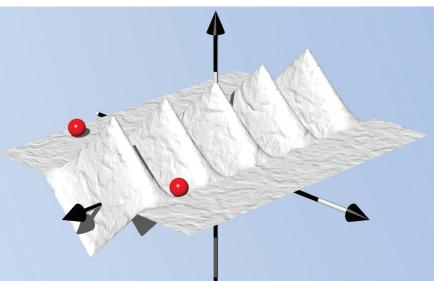
# **WORKING PAPERS**

# **Double Phase Estimator**

Towards a New Perception of the Subcarrier Component

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The subcarrier introduced in binary offset carrier (BOC) modulated signals has been perceived as a part of the signal code, as a source of ambiguity, and as a nuisance component that should be removed. This article introduces an advanced tracking algorithm that exploits a new conception of the subcarrier to fully benefit from the structure of BOC-modulated signals. odern global navigation satellite systems have adopted binary offset carrier (BOC) modulations to increase radio frequency (RF) compatibility among different signals and to improve ranging accuracy. BOC modulations use an additional signal component, the subcarrier, to move the signal power away from the signal center frequency and to obtain two main lobes displaced by  $f_{sub}$ , the subcarrier repetition frequency.

The subcarrier significantly reduces interference issues and leads to signals with sharp autocorrelation functions, i.e., with improved ranging capabilities. BOC signals are, however, characterized by multi-peaked correlation functions, and, as a result, secondary peak lock can occur. Thus, several techniques have been designed to avoid secondary peak lock and to track unambiguously the main signal correlation peak. The design of unambiguous BOC tracking algorithms has been strongly influenced by the perception of the subcarrier, which evolved significantly over the last two decades.

This article will first review the various perceptions of the BOC subcarrier and then describe a new view of the subcarrier along with an advanced tracking algorithm that exploits this subcarrier concept to fully benefit from the structure of BOC modulated signals.

# **Subcarrier Perception**

Modern GNSS signals can be modeled as the product of four components:

$$x(t) = d(t)c(t)s_b(t)\cos\left(2\pi f_{RF}t\right)$$
(1)

where

- *d*(*t*) is the navigation message containing the ephemerides and other navigation parameters
- *c*(*t*) is a pseudorandom sequence selected from a family of quasiorthogonal codes. *c*(*t*) is binary phase shift keying (BPSK)-modulated, i.e., each element of the code is represented as a constant (positive or negative) value.
- $s_b(t)$  is the subcarrier obtained by periodically repeating a basic waveform
- the cosine term is the carrier which is used to up-convert the signal to the RF,  $f_{\rm RF}$ .

**Figure 1** provides a schematic representation of the various signal components. (The figure ignores the navigation message, which slowly varies over time).

The code and carrier components are also present in legacy GPS signals and are usually processed using dedicated tracking loops: the delay lock loop (DLL) and the phase lock loop (PLL). The subcarrier has been introduced with the advent of Galileo (e.g., Open Service signal) and the modernization of GPS (e.g., L-band civil signal, L1C) to improve RF compatibility among different GNSS signals and increase ranging accuracy. (See the article by J. W. Betz, referenced in the Additional Resources section near the end of this article.)

The subcarrier has been considered in various ways by researchers and GNSS receiver designers, and its perception has been progressively changing over time. The subcarrier has been originally recognized as part of the ranging code, c(t), and jointly processed with it using a modified DLL. When considered in this way, the subcarrier modifies the code correlation function by leading to a narrower main correlation peak and by introducing secondary peaks.

Secondary peaks can be the source of ambiguity, and a standard DLL can erroneously lock on them, leading to biased pseudorange measurements. For this reason, one class of BOC tracking algorithms aimed to remove such ambiguity, for example, by introducing sentinel correlators as in the "Bump Jump" method detailed in the paper by P. Fine and W. Wilson, cited in Additional Resources. The sentinel correlators are used to verify that the peak locked by the DLL is the main one.

The subcarrier was then perceived as a nuisance component to be removed. In order to remove the subcarrier, several techniques were suggested such as the "SubCarrier Cancellation (SCC)" method described by P. Ward et alia (Additional Resources), side-band processing, and subcarrier pre-filtering. Although subcarrier removal can lead to robust signal tracking, the advantages brought by the subcarrier are generally lost in the process. In particular, these techniques usually lead to losses in terms of measurements accuracy, as they are unable to obtain code correlation functions with a narrow peak.

A new view of the subcarrier implies that the subcarrier should be considered similarly to the signal code and carrier in which a dedicated tracking loop is allocated to each component, including the subcarrier. Moreover, this approach suggests that the subcarrier should be exploited as a source of measurements in the same way as the code is used to generate pseudoranges and the carrier to produce carrier phase observations. For this reason, the subcarrier would also be used to generate subcarrier phase/delay measurements. Further, the subcarrier has characteristics intermediate between the code and carrier and, thus, can be processed by modifying techniques originally designed for these two signal components.

A fundamental step towards such a concept of the subcarrier was the "Double Estimator (DE)" suggested by M.S. Hodgart *et alia* (Additional Resources) where the code and subcarrier are processed independently. In particular, the subcarrier is processed similarly to the code using a dedicated loop, the "Subcarrier Lock Loop" (SLL).

This method introduces subcarrier "Early" and "Late" correlators and uses these to track the subcarrier component. Moreover, this approach employs the concept of "subcarrier delay," but only for tracking purposes. The subcarrier is not used for generating measurements, and code and subcarrier delays are recombined in order to generate pseudorange observations.

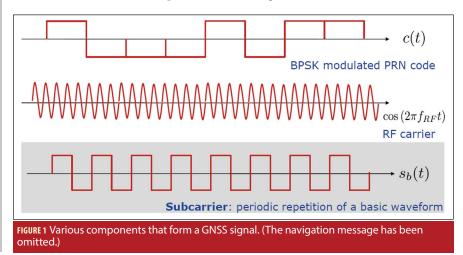
The DE method assimilates the subcarrier to an additional code superimposed through a multiplication of the BPSK-modulated ranging code. At the same time, a progressive understanding has emerged that the subcarrier is also similar to the carrier component. In the SCC method, two orthogonal sine waves are used as local subcarriers for the removal of the subcarrier component. In his Ph.D. thesis (see Additional Resources), C. Palestini used the subcarrier delay to smooth code measurements using a Hatch filter. J. Wendel and S. Hager (cited in Addition Resources) solved the subcarrier ambiguity problem using the LAMBDA method. These are approaches typically adopted for processing carrier phase measurements. The subcarrier is thus implicitly recognized as a source of measurements.

The "Double Phase Estimator (DPE)" described in the next section exploits this new conception of the subcarrier, which is approximated as a pure sinusoid and processed using a modified PLL, the "Subcarrier Phase Lock Loop (SPLL)."

# **The Double Phase Estimator**

The DPE exploits the commonalities between carrier and subcarrier. Moreover, it takes into account the effects of the receiver front-end. In particular, Equation (1) models the transmitted GNSS signal but does not consider several propagation and reception effects, such as those caused by the receiver front-end.

In an article from the author listed in Additional Resources, it is shown that, in the presence of front-end filtering, the subcarrier of the received signal can be effectively approximated as a pure sinusoid. When assimilated as a pure sinusoid, the subcarrier can then be tracked using a modified PLL, the SPLL, which



# **WORKING PAPERS**

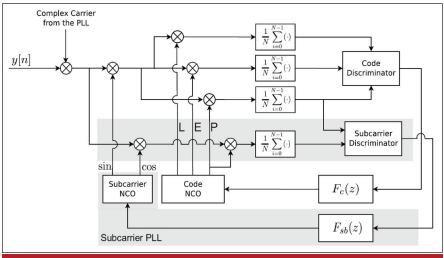
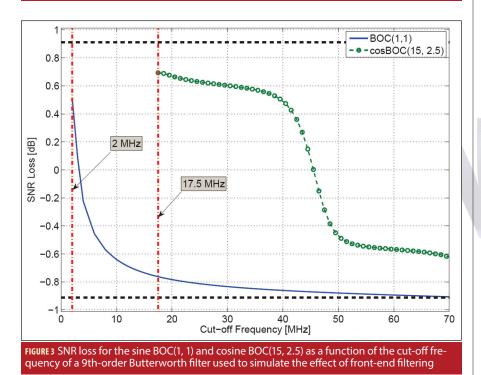


FIGURE 2 Schematic representation of the Double Phase Estimator



exploits the correlation of the input signal with two orthogonal local sinusoids.

**Figure 2** provides a schematic representation of the DPE. The signal at the input of the DPE is denoted by y[n]. Note that y[n] is a digital sequence obtained by sampling a filtered and down-converted version of the signal recovered by the receiver antenna. The residual signal Doppler effect is at first removed using the complex exponential generated by the PLL used to track the signal carrier. Code and subcarrier components are then processed independently using a standard DLL and a SPLL, respectively.

The SPLL uses an additional correla-

tor, denoted as *quadrature prompt correlator*, to estimate the residual subcarrier phase error. This correlator is obtained by correlating the input signal with a local replica orthogonal to the input signal subcarrier. This orthogonal subcarrier is obtained by delaying by  $T_{sub}/4$  the standard subcarrier used for the evaluation of the standard prompt correlator.  $T_{sub} = \frac{1}{2}$ 

$$T_{sub} = \frac{1}{f_{sub}}$$

is the subcarrier period.

In Figure 2, the standard subcarrier appears as a sine wave, whereas the orthogonal subcarrier is a cosine wave. This choice is dictated by the fact that a sine-phased BOC modulation is considered in Figure 2. When a cosine-phased modulation is processed, cosine and sine waves should be adopted for the generation of standard and quadrature components, respectively.

In Figure 2, the symbol *N* represents the number of samples used for the signal correlation, and  $F_c(z)$  and  $F_{sb}(z)$ denote the transfer functions of the filters adopted by the DLL and the SPLL, respectively. In equations (2) and (3), the symbols *P* and  $P_Q$  are used to denote the standard and quadrature prompt correlators. Two subcarrier discriminators can be used to extract the residual subcarrier delay error, as follows:

$$\varepsilon_{c}(\Delta\tau_{s}) = \frac{1}{2\pi f_{sub}} \arctan\left(\frac{\Re\{P_{Q}\}}{\Re\{P\}}\right) \quad (2)$$

$$\varepsilon_{nc}(\Delta \tau_s) = \frac{1}{2\pi f_{sub}} \arctan\left(\Re\left\{\frac{P_Q}{P}\right\}\right).$$
 (3)

Discriminator (2) is sensitive to residual phase errors from the PLL whereas (3) is non-coherent and can operate in the presence of residual phase errors.  $\Delta \tau_s$  is the residual subcarrier delay error, which leads to the discriminator outputs,  $\varepsilon_c$  and  $\varepsilon_{nc}$ , used to drive the SPLL.

### **Performance Analysis**

In the DPE, the local subcarrier is a pure sinusoid. When a wideband front-end is used, the subcarrier of the received signal can be effectively approximated as a square wave. Under these conditions, a mismatch between received and local subcarrier could occur, which can introduce a signal-to-noise ratio (SNR) loss. In the worst case, this loss is equal to

$$L_0 = \frac{8}{\pi^2} \to L_0 |_{dB} = -0.91 \text{ dB.}$$
 (4)

The SNR considered here is the coherent output SNR evaluated at the output of the prompt correlator. This SNR loss is present only in the absence of front-end filtering. An expression for the SNR loss ( $L_o$ ) can be found in the article by author cited in Additional Resources.  $L_o$  can become a gain when the signal is heavily filtered and the subcarrier of the received signal is more similar to a pure sinusoid than to an ideal square wave.

This fact clearly emerges in **Figure 3** where the SNR loss is shown as a func-

tion of the front-end bandwidth. More specifically, a 9th-order Butterworth filter was used to simulate the effects of front-end filtering, and  $L_0$  was evaluated as a function of its cut-off frequency. Figure 3 considers the cases of sine BOC(1, 1) and cosine BOC(15, 2.5) and reveals that the DPE provides a gain for the processing of wide-band BOC–modulated signals. This is the case of the cosine BOC(15, 2.5) modulation adopted for the Galileo Public Regulated Service (PRS) signal: a front-end with a total bandwidth greater than 45 megahertz is required to obtain an actual loss.

Note that signal band-limiting can also be introduced on the transmitter side. For example, the cosine BOC(15, 2.5) transmitted by the GIOVE-B satellite was characterized by a bandwidth of about 40 megahertz. In this case, the DPE will always provide better performance with respect to standard techniques.

The use of pure sinusoids as local subcarriers also affects the correlation functions evaluated by the receiver. In particular, in the DE and in the DPE techniques, a two-dimensional cross-correlation function is obtained:

$$R_{x}(\tau_{c},\tau_{s}) = \frac{1}{N} \sum_{n=0}^{N-1} y[n]c(nT_{s}-\tau_{c})\overline{s}_{b}(nT_{s}-\tau_{s})$$
<sup>(5)</sup>

where y[n] is the digital sequence at the front-end output and

$$T_s = \frac{1}{f_s}$$

is the sampling interval obtained as the inverse of the sampling frequency,  $f_s$ . Sequences  $c(nT_s - \tau_c)$  and  $\overline{s}_b(nT_s - \tau_s)$  are the code and subcarrier replicas locally generated by the receiver. Note that these two components are delayed independently by

 $\tau_c$  and  $\tau_s$ , the code and subcarrier delays tested by the receiver. The symbol '-' has been introduced on the local subcarrier to indicate that a sequence different from the signal subcarrier,  $s_b(\cdot)$ , can be used for the computation of cross-correlation (5). The DE uses a subcarrier equal to that of the input signal, whereas the DE uses sinusoidal subcarriers.

From the two-dimensional cross-correlation, it is possible to extract the following:

- the code correlation, when the subcarrier delay, τ<sub>s</sub>, is matched to that of the incoming signal y[n]
- the subcarrier correlation, when the code delay, τ<sub>c</sub>, is matched to that of the incoming signal y[n]
- the composite correlation, when the code and subcarrier delays are constrained to be equal,  $\tau_c = \tau_s$ . This is the correlation obtained by standard BOC tracking algorithms.

The following discussion only considers the subcarrier and composite correlations.

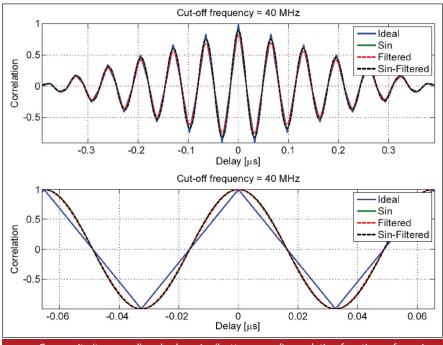
When a wideband front-end is used, the

DE and standard BOC tracking algorithms are able to obtain sharp cross-correlation functions close to the "Ideal" curves depicted in **Figure 4**. In the presence of front-end filtering, the correlation functions obtained using square waves as local subcarrier are strongly impacted. This fact clearly emerges from Figure 4, which shows in the top and bottom panels, respectively, the composite and subcarrier correlation functions of a cosine BOC(15, 2.5) signal in the presence of front-end filtering. Signal band-limiting has been simulated by filtering the input signal with a 9th-order Butterworth filter and cut-off frequency  $f_o = 40$  MHz.

In Figure 4, the curves denoted as "Ideal" and "Sin" are those obtained for the DE (square subcarrier wave) and for the DPE in the absence of filtering. When filtering is simulated, the correlation function computed using standard techniques are smoothed ("Filtered" curves in Figure 4). No significant difference can be observed for the DPE: Because only the first frequency component is retained, signal band-limiting has almost no effect on the correlation process, which implicitly performs filtering. The bottom part of Figure 4 reveals that when the front-end filter preserves only the main signal component, the DE and DPE operate on equivalent subcarrier correlation functions, which can be effectively modelled as pure cosine waves.

# **Tracking Jitter**

The tracking jitter is a measure of the uncertainty of the final output provided by a tracking loop. The following discussion analyzes and compares the tracking jitter of the SPLL used in the DPE with that of the SLL of the DE. In particular, the tracking jitter can be computed as (see the book chapter by A. J. Van Dierendonck, Additional Resources):



**FIGURE** 4 Composite (top panel) and subcarrier (bottom panel) correlation functions of a cosine BOC(15, 2.5) signal in the presence of front-end filtering. Front-end cut-off frequency,  $f_0 = 40$  MHz.

$$\sigma_{\tau} = \frac{\sigma_d}{G_d} \sqrt{2B_{eq}T_c}$$
(6)

where  $\sigma_d$  is the standard deviation of the discriminator output,  $B_{eq}$  is the loop equivalent bandwidth, and  $T_c = NT_s$  is the coherent integration time.  $G_d$  is the discriminator gain defined as

$$G_{d} = \frac{\partial \mathbb{E}\left[S(\tau)\right]}{\partial \tau} \bigg|_{\tau=0}$$
<sup>(7)</sup>

where  $S(\tau)$  is the discriminator input-output function.  $S(\tau)$  depends on the type of discriminator and can be computed using definitions (2) and (3).

The 2014 article by the author shows that the following equation gives the tracking jitter of the SPLL, for both coherent and non-coherent discriminators:

$$\sigma_{\tau} = \frac{1}{2\pi f_{sub}} \sqrt{\frac{\frac{2B_{eq}T_{c}}{C}}{\frac{1}{\frac{1}{N}N_{0}B_{Rx}}L_{0}}} \left(1 + \frac{1}{\frac{1}{\frac{1}{N}N_{0}B_{Rx}}L_{0}}\right) \approx \frac{1}{2\pi f_{sub}} \sqrt{\frac{B_{eq}}{\frac{1}{N}L_{0}}} \left(1 + \frac{1}{2\frac{C}{N_{0}}T_{c}L_{0}}\right)$$

where  $B_{Rx}$  is the bandwidth of the receiver front-end and  $\frac{C}{N_0}$  is the carrier-to-noise density power ratio of the signal tracked by the SPLL. The last approximation in (8) was obtained by exploiting the hypothesis that the front-end bandwidth is approximately equal to half the sampling frequency, as follows:

$$B_{Rx} \approx \frac{f_s}{2} = \frac{1}{2T_s} \longrightarrow \frac{1}{N} B_{Rx} \approx \frac{1}{2NT_s} = \frac{1}{2T_c}.$$
 (9)

The tracking jitter of the output of the SLL used by the DE is given by

$$\sigma_{\tau}^{SLL} = \frac{1}{f_{sub}} \sqrt{\frac{B_{eq}d_s}{8C / N_0}} \left( 1 + \frac{1}{\frac{C}{N_0}T_c \left(1 - 2d_s\right)} \right)$$
(10)

and depends on  $d_s$ , the subcarrier Early-minus-Late chip spacing. As previously mentioned, the DE treats the subcarrier similarly to the code, and two additional subcarrier correlators are used to track the main peak of the subcarrier correlation function. In Equation (10),  $d_s$  is normalized by the subcarrier period,  $T_{sub}$ , and thus is unitless.

**Figure 5** compares the tracking jitter of the SLL with that of the SPLL. The curves shown in the figure were obtained using the parameters listed in **Table 1**.

The performance of the SLL strongly depends on the Earlyminus-Late spacing adopted: for narrow  $d_s$ , the SLL outperforms the SPLL, which becomes preferable for  $d_s$  greater than 0.25. For  $d_s = 0.25$ , the SLL and SPLL have similar performance as predicted by (8) and (10) when

$$L_0 = \frac{8}{\pi^2}$$

The curves in Figure 5 were obtained in the least favorable case for the SPLL, i.e., in the absence of front-end filtering.

Figure 5 also provides the tracking jitter of the DLL of the SCC technique. Note that when recombining subcarrier and

code measurements as in the DE, the dominant source of error stems from the SLL. Thus, we can effectively approximate the final tracking jitter using the subcarrier delay estimate. For this reason, the tracking jitter of the SCC can be compared with that of the SLL and SPLL.

Because no theoretical results are currently available for the SCC tracking jitter, Figure 5 only presents simulation results. The algorithm detailed in the article by P. Ward et alia was implemented and used for the analysis: Subcarrier Cancellation also requires the computation of Early and Late correlators for the DLL and the performance of the loop strongly depends on the Early-minus-Late chip spacing,  $d_s$ , of these two correlators.

The results provided in Figure 5 indicate that the SCC is always outperformed by the other techniques. This anticipated

outcome is due to the subcarrier removal operated by the SCC technique. Although the SCC uses a sinusoidal representation of the subcarrier, its performance is significantly worse than that of the DPE.

# **Real Data Processing**

In order to test the effectiveness of the DPE, cosine BOC(15, 2.5) signals collected from the GIOVE-B satellite were used. Note that the European Space Agency decommissioned GIOVE-B satellite in July 2012 and that the dataset used in this paper was collected on November 5, 2011. The use of such a dataset is justified by the fact that it contains valid cosine BOC(15, 2.5) data

with a known pseudorandom noise (PRN) code. Thus, the use of this dataset allows one to test the DPE for both the sine BOC(1, 1) and cosine BOC(15, 2.5)modulation broadcast in the Galileo E1 band. The cosine BOC(15, 2.5) signals transmitted by the currently operating Galileo satellites are encrypted, and use of them requires codeless techniques.

(8)

A complete analysis of the tracking results obtained for the sine BOC(1, 1) signal can be found in the article from the author listed in Additional Resources. The following discussion addresses only the case of

Parameter	Value	
Sampling frequency, $f_s$	8 MHz	
Integration Time, $T_c$	4 ms	
Modulation Type	sine BOC(1,1)	
DLL order	1	
DLL bandwidth	1 Hz	
SPLL order	1	
SPLL bandwidth	1 Hz	
Table 1 Parameters adopted for the tracking           jitter analysis in Figure 5.		

Parameter	Value
PLL order	3
PLL bandwidth	10 Hz
DLL order	2
DLL bandwidth	5 Hz
SPLL order	2
SPLL bandwidth	5 Hz
E1a Integration Time (before bit sync)	2 ms
E1a Integration Time (after bit sync)	10 ms
Table 2 Parameters adopted for the process- ing of the GIOVE-B E1a signal	

the cosine BOC(15, 2.5) modulation. In particular, the DPE is able to effectively process the E1a signal. **Figure 6** provides sample results including several metrics that indicate the proper functioning of the proposed technique. **Table 2** lists the parameters used for the processing of the GIOVE-B E1a signal.

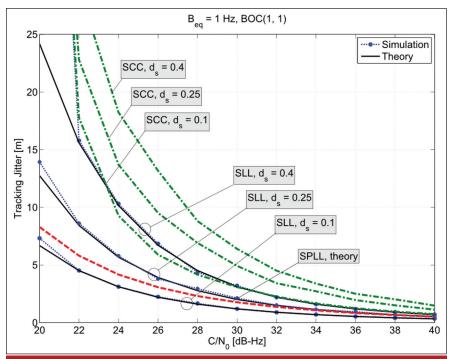
Figure 6a shows the amplitudes of the Prompt, Early, and Late correlators used by the DLL, coupled with the SPLL: After an initial transient period, the amplitude of the Prompt correlator is maximized whereas Early and Late correlators assume similar magnitudes.

Figure 6b provides the filter outputs of the three loops used for signal tracking. Each output is normalized by the fundamental frequency of the component tracked: the carrier Doppler by the GPS L1 center frequency, 1575.42 MHz; the DLL filter output by the nominal code rate, 2.5575 megahertz; and the SPLL filter output by the subcarrier rate, 15.345 megahertz.

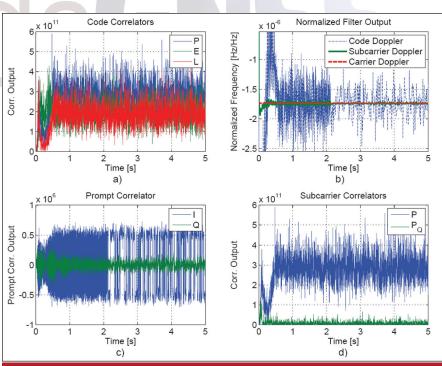
The normalized filter outputs assume similar values indicating the possibility of carrier aiding: The normalized carrier Doppler can be used to help process the code and subcarrier components. As expected the code estimates are the nosiest. After about two seconds, the secondary code on the E1a signal is recovered and bit synchronization is achieved. Thus, the integration time is increased from 2 to 10 milliseconds.

The latter effect can be clearly seen in the code rate estimates in Figure 6b and in Figure 6c, which shows the in-phase and quadrature components of the Ela Prompt correlators. After bit synchronization, the secondary code is removed and the navigation bits can be extracted from the in-phase components of the Prompt correlator.

Finally, Figure 6d compares the magnitude of the  $P_Q$  correlator with that of the Prompt correlator. After an initial transient, the magnitude of  $P_Q$  is minimized and all the signal energy is concentrated in the Prompt correlator. This shows the ability of the Double Phase Estimator to properly track the different components of the cosine BOC(15, 2.5) modulation.









#### Conclusions

In this article, various ways of considering the subcarrier component have been briefly reviewed. In particular, the discussion promotes the idea that the subcarrier has its own "dignity." In this respect, the subcarrier should be processed using a dedicated tracking loop and considered as a source of measurements.

Furthermore, the subcarrier has characteristics intermediate between the code and carrier, and thus it can be processed adapting algorithms originally designed for these two signal components. The Double Phase Estimator exploits the "carrier" nature of the subcarrier, which is processed using a modified PLL, the SPLL. The DPE is an effective alternative to the DE and can achieve improved performance in the presence of front-end filtering.

#### **Manufacturers**

The GIOVE-B cosine BOC(15, 2.5) signals were recorded using an NI PXI-5663 RF signal analyzer from **National Instruments Corporation**, Austin, Texas USA.

# **Additional Resources**

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[3] Fine, P., and W. Wilson, "Tracking algorithm for GPS offset carrier signal"," *Proceedings of the National Technical Meeting of the Institute of Navigation (ION NTM 1999),* San Diego, CA, pp. 671–676, January 1999

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# Letter

# **Satcom Costs Slow Airliner Tracking with GNSS**

I always enjoy reading your comments. However, I have some comments on your last article ("Flying Blind," Thinking Aloud, MarchApril 2015).

- 1. MOPS stands for Minimum Operational Performance Standards, not specifications.
- 2. ICAO does not produce MOPS, RTCA does.
- 3. MOPS are not mandatory until ordered by FAA or another nation.

Most airlines that travel over oceans or other areas where there are no ground communications are equipped with ACARS and can communicate with the ground through satellite. The cost of transmissions is too expensive to transmit location info all the time. A line-of-sight link is used domestically that can transmit location info (this operation is called ADS (automatic dependent surveillance).

Several years ago the USAF had a program for a radar in space that could monitor all aircraft in a given coverage area. I think this may have been cancelled when the threat changed from aircraft to missiles. Plus we have other ground radars (satellite also for missiles) that can detect aircraft and missiles earlier before they reach the US.

Bottom line is that the cost of aircraft equipage is not the main problem but the cost of transmission via satellite is. Domestic location is not a problem using secondary radar, Mode S, and other links that aircraft have today.

#### Larry Chesto

Aviation Consultant Williamsburg, Virginia

*Your comments and suggestions about the magazine and its contents are welcome at <glen@insidegnss.com>***IG** 

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#### Author



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Prof.-Dr. Günter Hein

serves as the editor of the Working Papers column. He served as the head of the EGNOS and GNSS Evolution Program Depart-

ment of the European Space Agency and continues to advise on scientific aspects of the Navigation Directorate as well as being a member the ESA Overall High Level Science Advisory Board. Previously, he was a full professor and director of the Institute of Geodesy and Navigation at the Univer-sität der Bundeswehr München. In 2002, he received the Johannes Kepler Award from the U.S. Institute of Navigation (ION) for "sustained and significant contributions" to satellite navigation. He is one of the inventors of the CBOC signal.